# PID design with bio-inspired intelligent algorithms for high order systems

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**Abstract**—In this paper we have proposed the application of PSO and BFO intelligent algorithms to find the optimal parameters of a PID controller, applied in the control of a high order process. The case of PID design for high order systems with time delay is also considered, since time delays introduce problems in the stability and performance of the control system. A fixed parallel structure of PID controller and four most common integral performance indexes are considered as optimization functions in this paper. The evaluation of the proposed methods is performed by using the classical performance measures in time domain.

*Keywords*—BFO algorithm, Integral performance index (IAE, ISE, ITAE, ITSE), PID controller, PSO algorithm.

### I. INTRODUCTION

MANY processes in industry are characterized by large time constants and time delays. These processes are usually represented in process control by high order mathematical models with or without time delays.

Delays are usually present in control systems as delays in computing processes or as delays in information transmission. They are very common in chemical, biological, information, and also measuring processes. Time delays introduce problems in process control due to decrease of robustness and performance deterioration, which affect the system's stability.

PID controllers, predictive control, and time-delay compensators are some of the several invented control methods, for control of high order time-delay processes [1]. Among them, PID controllers have found wider application. Their popularity is related to the fact that they are simple to understand and to operate by operators, and are effective and robust in control. Even though, approximately 95% of the control schemes in practice are based on PID controllers, finding the right parameters of these controllers to achieve maximum control performance, poses a challenge in itself. There exist many methods for the calculation of the PID optimal parameters that help to obtain a specific characteristic of process time response. To verify the effectiveness of various methods for PID controllers, the comparison is usually

made by analyzing the transient characteristics of the system. The characteristics obtained by tuning the PID parameters, often do not meet the control performance criteria defined by the designer. This is mainly due to the fact that many processes in nature are of high order, and are characterized by time delays and nonlinearity [2]. For this reason, latest research is focused on optimization methods based on intelligent algorithms, which result very efficient in solving difficult optimization problems. Evidence of successful application of these algorithms can be found in [3]-[11]. Algorithms, inspired by characteristics and organized behaviors of organisms and microorganisms in nature, have recently achieved an increasing interest. Among these algorithms, we have chosen Particle Swarm Optimization (PSO) and Bacterial Foraging Optimization (BFO) algorithms as optimization methods. These two algorithms are the main focus of this work and our proposal is to apply them in finding the optimal PID parameters for a high order control system. The case related to the presence of time delays in high order systems will also be considered.

Previous research has been conducted on application of intelligent techniques such as Genetic Algorithm (GA) and Differential Evolution (DE) for the optimization of PID controller parameters for high order systems and systems with time delay [12]. PSO is proved to be more efficient than GA algorithm method and also has less computation codes. BFO algorithm is more complex and requires more computational capacity compared to PSO algorithm [3].

Four well-known integral performance criterions are proposed as optimization functions in our case. These performance indexes will be used to obtain the coefficients of PID controller, and then process transient responses will be analyzed and compared with the methods of obtaining PID coefficients from PSO and BFO algorithms.

The structure of the article is as follows. Section II presents the proposed control schemes for the high-order process with/without time delay, transient response measures and also the integral performance indexes used as optimization (cost) functions to find the coefficients of PID controllers. In section III, PSO and BFO algorithms, and their application in finding the coefficients of PID controllers are treated. The process models that will be considered for various simulations with classical methods (IAE, ISE, ITAE, ITSE) and intelligent methods (PSO and BFO) is presented in section IV. Conclusions obtained from simulations are presented in

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section V. Algorithms and computational simulations are performed in MATLAB environment.

# II. OPTIMIZATION FUNCTIONS

# A. Control Scheme

The proposed control scheme for finding the optimal coefficients of PID controller is illustrated in Fig. 1. Signals presented in the control scheme are: reference signal R(s), that is a step unit function in our case, output signal of the system Y(s), control signal U(s), and error signal E(s) derived from E(s) = R(s)-Y(s).



Fig. 1 Proposed control scheme for the process. Proposed PID controller is in its parallel form, provided by the algorithm:

$$u(t) = K_p e(t) + K_i \int_0^t e(\tau) d\tau + K_d \frac{d}{dt} e(t)$$
(1)

where

u(t)-control signal in time domain

 $K_p$  -proportional coefficient, a tuning parameter

 $K_i$  -integral coefficient, a tuning parameter

 $K_d$  -derivative coefficient, a tuning parameter

e(t) -error signal in time domain

In Fig. 2 is presented the typical PID controller structure in its parallel form. The process that will be studied is a single input-single output (SISO) high order system with or without time delay, which represents many processes in industry. The delay term represents the general effect of the plant inertia, and its high order and parameter distribution [13].



Fig. 2 Structure of PID controller

The mathematical model of delay term  $e^{-Ls}$  according to [14] can be approximated by a rational transfer function of the form:

$$G_{i}(s) = \frac{1}{\left(1 + \frac{Ls}{i}\right)^{i}}, \ i = 1, 2, \dots$$
(2)

which is an *i*-th order truncation of expression

$$e^{-Ls} = \lim_{i \to \infty} \frac{1}{\left(1 + Ls/i\right)^i} \,. \tag{3}$$

### B. Transient Response Measures

Analysis for the process transient response in time domain is done through performance quantities [15] like:

-Rising time  $t_r$ : time required for the output of the system to reach 90% of its final value  $h(\infty)$ .

-Settling time  $t_s$ : time after which the output remains within  $\pm 2\%$  of the final value  $h(\infty)$ .

-Peak value  $h_{max}$ : peak value of the transient response h(t) of the process.

-Peak time  $t_{peak}$ : time required for the transient response h(t) to reach the peak value  $h_{max}$ .

-Overshoot  $M_r(\%)$ : output value exceeding final, steady-value of the process, expressed in percentage.

Rising and settling times are measures of response speed of the system. Overshoot, peak value, and peak time are related measures to the quality of response.

## C. Integral Performance Criteria

In classical control methods, the performance of the entire control system can be estimated quantitatively using a single parameter that is the integral quality criterion J. This performance index is useful in treating optimization of parameters and obtaining optimal control designs. According to [16], a system is considered as an optimal control system when the system parameters are tuned to achieve an integral criterion ekstremum, which is usually a minimum value. Integral criterion should always be a positive number or equal to zero  $J \ge 0$ . The best achievable control system is the system that minimizes this criterion. The general form of the integral performance criterion is:

$$J = \int_{0}^{1} f(e(t), r(t), y(t), t) dt$$
(4)

where f is a function of error, input, ouput signals and time. The most common integral criterions are:

- Integral of squared error  $ISE = \int_{0}^{T} e^{2}(t)dt$  (5)

where *T* is a finite time, chosen arbitrarily, in order for the integral to approach the final stabilized value of the system. Generally *T* is chosen as equal to  $t_s$ -settling time.

-Integral of absolute error 
$$IAE = \int_{0}^{T} \left| e(t) dt \right|$$
 (6)

-Integral of time multiplied absolute error  $ITAE = \int_{0}^{1} t \left| e(t) dt \right|$ (7)

-Integral of time multiplied squared error  $ITSE = \int_{0}^{T} te^{2}(t)dt$  (8)

### **III. INTELLIGENT ALGORITHMS**

Nature is the perfect example of optimization, because many organisms and microorganisms in nature always interact or collaborate to find the optimal strategy for a specific natural process. The real interesting fact about nature inspired algorithms is that they receive their inspiration from naturerelated behaviours. These bio-inspired algorithms have found recent applications in computer networks, robotics, control systems, security systems, power systems and many more [17].

# A. PSO Algorithm

The PSO is created by Eberhart and Kennedy in 1995 [18], [19]. The method is suitable for solving nonlinear problems and to give optimal solutions [20]. This algorithm is inspired by natural behavior of animals, such as organized behavior of birds in flock for finding food [21], [22]. PSO algorithm has simple computations because it does not require gradient calculations. Since it is a stochastic technique with a large number of candidate solutions, it is unlikely to be stuck at a local minimum [20]. Its suitability in distributed computing environments makes it a helpful tool for online controller tuning [3].

PSO algorithm operates using a population (called swarm) of a potential candidate solution (called particles). These particles move around a search space according to a specific routine (law). Movements of particles are guided by their best known position in the search space and also the best known position by the whole flock. When better positions are detected, these positions guide the further movement of the particles. The process is repeated until a satisfactory solution is reached. In this optimization method, a set of particles are placed in a *d*-dimensional space with a random specified speed and position. The initial position of the particle is taken as the best position in the beginning and then particle speed is reassessed based on the experience of other particles of the flock (population).

From [23], PSO algorithm elements are: -the i-th particle in the population represented by:

 $x_i = (x_{i1}, x_{i2}, x_{i3}, \dots x_{id})$ 

in the *d*-dimensional space.

-previous best positions of the *i*-th particle represented by:

$$P_{opt} = (P_{opt_{i,1}}, P_{opt_{i,2}}, P_{opt_{i,3}}, \dots P_{opt_{i,d}})$$
(10)

-the index of the best particle in the swarm  $G_{opt,d}$ -the speed of the *i*-th particle represented by:

$$V_i = (v_{i1}, v_{i2}, v_{i3}, \dots v_{id})$$
(11)

-reassessed speed and distance from  $P_{opti,d}$  in  $G_{opti,d}$  given by the law:

$$V_{i,m}^{t+1} = W \cdot V_{i,m}^{t} + C_1 \cdot rand() \left( P_{opt_{i,m}} - X_{i,m}^{t} \right) + C_2 \cdot rand()$$

$$\left( G_{opt_m} - X_{i,m}^{t} \right) - X_{i,m}^{(t+1)} = X_{i,m}^{(t)} + V_{i,m}^{(t+1)}$$
for  $i=1,2,3,...n$ ;  $m=1,2,3,...d$ 

$$(12)$$

where *m* number of particles in swarm, *d* dimension index, *t* iteration index,  $V_{i,m}^{(t)}$  the particle speed in iteration *i*, *W* weighting factor of inertia,  $C_I, C_2$  acceleration constants, *rand()* random number between 0 and 1,  $X_{i,m}^{(t)}$  actual position of the *i*-th particle in iteration.

Typically the number of particles in swarm is 20-40 to be

able to solve most of the problems [24]. Constants  $C_1$ ,  $C_2$ represent the degree of influence of individual and group experience on the speed adjustment respectively. When  $C_1$  is zero, the particle velocity is completely free from the impact of individual experience. In this case, it will soon converge, but it can easily fall into local minimum, and not into global optimum. When  $C_2$  is zero, the particle velocity is completely free from the impact of group experience. This allows each particle to adjust its position according to their own experience, and in this case we don't receive an effective solution. Therefore, in order to ensure global convergence of particle swarm speed and fitness, we need appropriate  $C_1$  and  $C_2$  values [24]. Inertia weight W affects the capability of the global search. When W is large, the speed of the particles in the iterative process will be large, global search ability will be stronger. Conversely, when the W is small, the speed of particles in the iterative process will be small, local search capability enhanced, and global search capability weakened. Therefore, appropriate inertia weight can make PSO have better global search capability, while also having fast convergence rate. In the beginning of the algorithm, PSO has no inertia weight, meaning that the inertia weight is a fixed value of 1. However, in the process of the convergence of the particles, the inertia weight should be a dynamic value. So, at the beginning of the algorithm, the particle should have a large global search capability, to allow the rapid convergence of the particle swarm and to find the approximate location of the optimal solution. In the end of the algorithm, it's needed to increase the local search ability of particles, in order to achieve the optimal solution of the particles. Typically inertia weight of initial value is 0.9, the minimum value is 0.4. Random number is used to keep impressing particles with the randomness of the flight, to make sure particles can jump out of bondage, enlarging the searching scale [24].

The flowchart of PSO algorithm is illustrated in Fig. 3.

### B. BFO Algorithm

(9)

BFO is based on research conducted by K.M. Pasino [25], [26], related to development and behavior of E.coli bacteria. This algorithm is gaining popularity in research community, due to its effectivenes in solving difficult real-world optimization problems. Some successful applications of this algorithm can be found in optimal control, transmission loss reduction, machine learning, etc. Usually BFO performance is poorer than PSO or GA algorithms due to it greater dimensions of searching space [27]. BFO due to its unique dispersal and elimination technique can find favourable regions when the population involved is small. The algorithm of this technique is composed of two steps: initialization and iterative algorithm for optimization [28].



Fig. 3 Flowchart of PSO algorithm

In this optimization method there are four typical behaviors that imitate nature [29]:

Chemotaxis This process resembles the movement of a bacterium (E.coli) through swimming and displacement via flagella. Biologically an E.Coli can move in two different ways. It can swim for a period of time in one direction, or it can move alternatively between two modes of movements throughout lifetime. To represent a shift we use a casual direction with a given unit size by  $\theta(i)$ . This presentation is used to determine the movement direction after a displacement. In particular:  $\theta^{l}(j+1,k,l) = \theta^{l}(j,k,l) + C(i) \cdot \theta(j)$ where  $\theta^{i}(j,k,l)$  represents the *i*-th bacterium in the *j*-th chemotaxis, the k-th reproduction, the l-th elimination and dispersal step C(i) is the size of the step taken in a random direction specified by the unit size  $\theta(j)$ . N<sub>s</sub> represent the swimming length after which tumbling of bacteria will be undertaken in a chemotactic loop and  $N_c$  the number of iterations to be undertaken in a chemotactic loop  $(N_c > N_s)$ .

*Swarming* E.coli bacteria organize themselves into wellstructured colonies with high environmental adaptability using a complex communication mechanism. To create the colonies, bacteria produce signals which are attractive to each other. Analytical presentation of this process is:

$$J_{cc} = (\theta, P(j,k,l)) = J_{cc}^{i}(\theta, \theta^{i}(j,k,l)) = \sum [D_{attract} \cdot e^{(-W_{attract} \cdot \sum (\theta_{m} - \theta_{m}^{l})^{2}}] + \sum [H_{repellant} \cdot e^{(-W_{repellant} \cdot \sum (\theta_{m} - \theta_{m}^{l})^{2}}]$$

$$(13)$$

where  $J_{cc}(\theta, P(jk, l))$  is the value of the optimization function

(to be minimized) to represent a cost function that depends on time. *S* is the total number of bacteria; *P* is the number of parameters to be optimized, which are present in each bacteria and  $D_{attract}$ ,  $W_{attract}$ ,  $H_{repellant}$ ,  $W_{repellant}$ , are different coefficients that should be chosen carefully.

*Reproduction* Less healthy bacteria die and each healthier bacteria split into two daughter bacteria, each located in the same position. In this process  $N_{re}$  represents the maximum number of reproduction to be undertaken.

*Elimination and Dispersal* In the local environment, it is possible that the bacteria life of a population can change gradually (e.g. through the consumption of nutrients) or abruptly from other influences. It may happen that in a zone all the bacteria die, or a group is dispersed in a new environment. They can destroy the progress of chemotactic effect, but they can also help the effect, if dispersal occurs in areas with good food sources. From a broader perspective, elimination and dispersal are part of the motion behavior of the population for long distances.  $N_{ed}$  represents the maximum number of elimination and dispersal events to be imposed over the bacteria,  $P_{ed}$  probability with which the elimination and dispersal will continue.

In the first step are set the initial values of the algorithm parameters *P*, *S*,  $N_{s}$ ,  $N_{c}$ ,  $N_{re}$ ,  $N_{ed}$ ,  $P_{ed}$ , C(i),  $\theta(j)$ ,  $D_{attract}$ ,  $W_{attract}$ ,  $H_{repellant}$ ,  $W_{repellant}$ . In the second step, the bacterial population (chemotaxis process), swarming, reproduction, elimination and dispersal are modeled. By updating the  $\theta^i$ , automatically results in updating the *P* [28]. Flowchart of BFO algorithm [30] is illustrated in Fig. 4.

# IV. SIMULATION RESULTS

In this study we have taken a high (forth) order process, which has a characteristic with many oscillations. Two cases are considered: first case with no time delay ( $G_1$ ) and second case with time delay ( $G_2$ ), represented by the following models in Laplace domain.

$$G_{1}(s) = \frac{10}{s^{4} + 10s^{3} + 35s^{2} + 50s + 24}$$

$$G_{2}(s) = \frac{10}{s^{4} + 10s^{3} + 35s^{2} + 50s + 24}e^{-3s}$$
(14)

As shown in Section II.A, the delay in time will appear in a rational function form:

$$G_{delay, l}(s) = e^{-3s} = \frac{l}{3s+l}$$
(15)

Resulting from above, the transfer function  $G_2$  to be considered during the simulations is:

$$G_{2}(s) = \frac{10}{3s^{5} + 31s^{4} + 115s^{3} + 185s^{2} + 122s + 24}$$
(16)

Usually, to achieve an optimal PID controller, the four transient response measures, such as rise time  $t_r$ , steady state error  $E_{ss}$ , settling time  $t_s$ , and overshoot  $M_r$  are used. The optimization function in this case is:

$$J = (1 - e^{-\beta})(M_r + E_{ss}) + e^{-\beta}(t_s - t_r)$$
(17)

where  $\beta$  is a weighting factor ( $\beta < 0.7$  to decrease settling time  $t_s$  and rise time  $t_r$  and  $\beta > 0.7$  to decrease  $M_r$  and  $E_{ss}$ ).



Fig. 4 Flowchart of BFO algorithm

This cost function was used in [20] in the case of PSO algorithm. The inverse of function (17) can be used as cost function in the case of BFO algorithm. In the proposed control scheme (Fig. 1), it is intended to tune the three coefficients of PID controller, in order to obtain the best (optimal) output results. Our proposal is to use integral criterions as cost functions, and to evaluate the performance of various combinations of PID coefficients in a 3-dimensional search domain. Each point in this 3-dimensional search domain for the proposed algorithms, represents a certain combination of [Kp,Ki,Kd] coefficients, for which a certain transient response of the system is achieved. In the proposed PSO and BFO algorithms, used to achieve the minimization of the integral performance indexes, the PID parameters are used as input values and as output is used the optimization value of the PID controller model (18).

Function [J]=integral criteria  $(K_d, K_p, K_i)$  (18)

# A. Classical Approach

Using IAE, ISE, ITAE, ITSE integral criterions, treated in Section II.C, in Fig. 5 are obtained the transient responses for processes  $G_1$  and  $G_2$ . Executing the algorithms in [31], we obtain the corresponding PID controllers for our integral performance criterions.



Fig. 5 Step responses for classical algorithms: a) process  $G_1$ , b) process  $G_2$ .

PID controllers, obtained by the classical algorithms for processes  $G_1$  and  $G_2$  are respectively shown in Table I.

Table I. PID controllers obtained by classical algorithms for rocess  $G_1$  and  $G_2$ .

Performance	0 <u>2</u> .	Coeffici	Coefficients of PID controllers				
Index	Process	$K_p$	$K_i$	$K_d$			
105	$G_1$	7.084	8.522	10.33			
ISE	$G_2$	7.616	cients of PID controllers $K_i$ $K_d$ 8.522         10.33           3.112         18.49           4.091         5.353           1.699         10.42           5.322         6.186           2.165         12.50           3.180         3.100           1.427         6.808	18.49			
IAE	$G_1$	7.262	4.091	5.353			
	$G_2$	7.579	1.699	10.42			
TROP	$G_1$	7.492	5.322	6.186			
ITSE	$G_2$	7.941	2.165	12.50			
ITAE	$G_1$	5.833	3.180	3.100			
ITAL	$G_2$	6.394	1.427	6.808			

# B. Intelligent PSO and BFO algorithms approach

In order to find the PID controllers coefficients by the intelligent algorithms PSO and BFO, in this study we have used the 3-dimensional search domain where the  $K_p$ ,  $K_i$ ,  $K_d$  values are the three dimensions of searching domain. In both\_algorithms, the four integral criterions of time domain, treated in Section II.C, were chosen as optimization functions. The algorithms were executed in Matlab environment where as cost functions were used:

- ISE: J=e'\*e\*dt

- IAE : J = sum(abs(e)\*dt)

- ITSE: J = (t. \*e'\*dt)\*e;

- ITAE: *J*=*sum*(*t*'.\**abs*(*e*)\**dt*)

In order to achieve the optimization goal, the PSO and BFO algorithm parameters should be selected properly [21]. The initial constants for the computing PSO algorithm were taken= m=25, W=0.7,  $C_1 = C_2=1.5$ . Upon execution of PSO algorithm, at Matlab prompt are displayed the [Kp, Ki, Kd] items of search domain, which is the final point of global optimum noted as  $g_{opt}$ , that corresponds to the minimum value of cost function, noted as  $f_{opt}$ .

Coefficients of PID controllers, obtained by intelligent PSO algorithm are shown in Table II. In Table II are also shown the best (minimum) values of cost functions (integral criterions). The constants used for the initialization of the computing program in BFO algorithm are chosen as  $D_{attractant}=0.01$ ,  $W_{attractant}=0.01$ ,  $H_{repellant}=0.01$ ,  $W_{repellant}=0.01$ .

Table II. PID controllers obtained by PSO algorithms for processes  $G_1$  and  $G_2$ .

Performance	Process	Coefficie	f <sub>opt</sub>		
Index		$K_p$	$K_i$	$K_d$	
PSO-ISE	$G_1$	5.9979	4.5977	10.045	0.4167
	$G_2$	5.8358	2.4775	7.7808	1.3484
PSO-IAE	$G_1$	6.6516	3.0712	4.8638	0.8184
	$G_2$	5.9132	3.2248	8.4042	3.3861
PSO-ITSE	$G_1$	5.8190	4.5353	5.0056	0.1566
	$G_2$	6.3134	2.2741	8.7790	1.2883
PSO-ITAE	$G_1$	8.3095	4.2609	4.2611	0.7443
	$G_2$	4.4448	1.5272	5.5659	4.2088

Table III presents the values of PID controller coefficients obtained by BFO algorithm, and the corresponding minimum values of cost functions for processes  $G_1$  and  $G_2$ .

Table IV presents the transient response measures for processs  $G_1$  and  $G_2$  for the three investigated methods.

Table III. PID controllers obtained by BFO algorithms for process  $G_1$  and  $G_2$ 

Performance Index	Process	Coefficie	f <sub>opt</sub>		
		$K_p$	$K_i$	$K_d$	
DEO ME	$G_1$	6.8883	4.4345	7.0298	0.4042
BFO-ISE	$G_2$	4.4140	1.5289	3.3416	1.6023
BFO-IAE	$G_1$	7.1812	6.2277	6.6093	0.7874
	$G_2$	5.1516	1.6386	3.9190	2.1803
BFO-ITSE	$G_1$	7.1376	4.4838	4.7165	0.1403
	$G_2$	5.9585	2.8791	8.0138	0.8610
BFO-ITAE	$G_1$	6.4745	4.5093	3.4626	0.5943
	$G_2$	5.7687	2.8277	8.0427	0.9163

Fig. 6 presents the step responses for processes  $G_1$  and  $G_2$  obtained by PSO algorithm for various optimization functions.





Fig.6 Step responses for PSO algorithms: a) process  $G_1$ , b) process  $G_2$ .

Characteristics	Method	Process G1			Process G2				
		ISE	IAE	ITSE	ITAE	ISE	IAE	ITSE	ITAE
Rising time t <sub>r</sub>	Classical	4.073	5.996	5.451	8.335	9.398	13.222	11.734	17.489
	PSO	0.425	0.655	0.665	0.609	1.633	1.510	1.520	2.452
	BFO	0.520	0.523	0.625	0.723	2.389	2.118	1.557	1.587
Settling time t <sub>s</sub>	Classical	84.948	36.467	54.598	35.841	131.74	64.118	115.39	73.285
	PSO	8.092	4.550	5.786	3.950	14.479	15.028	10.848	12.634
	BFO	5.564	5.326	4.059	4.371	10.126	8.866	15.057	15.472
Overshoot M <sub>r</sub> (%)	Classical	22.903	10.348	14.461	5.208	20.356	8.940	13.421	4.515
	PSO	15.177	4.541	5.711	19.196	12.298	20.150	8.428	8.064
	BFO	10.663	15.052	12.066	14.342	17.141	16.917	17.408	16.118
Peak value h <sub>peak</sub>	Classical	1.229	1.104	1.145	1.052	1.206	1.089	1.134	1.045
	PSO	1.152	1.045	1.057	1.192	1.123	1.202	1.084	1.081
	BFO	1.107	1.151	1.121	1.143	1.172	1.169	1.174	1.161
Peak time t <sub>peak</sub>	Classical	10	14	13	18	23	30	28	38
	PSO	0.930	1.295	3.442	1.393	4.184	4.409	3.412	7.845
	BFO	1.096	1.162	1.362	1.628	5.920	5.204	4.237	4.902

Table IV. Transient response characteristics for processes G1 and G2

Fig.7 presents the process transient responses obtained by BFO algorithm, for various optimization functions.



Fig. 7 Step responses for PSO algorithms: a) process G<sub>1</sub>, b) process G<sub>2</sub>.

Fig. 8 presents the best transient responses of process obtained by ITAE, PSO-ITSE, BFO-ITSE algorithms.

# V. CONCLUSION

Based on the performed simulations, we arrive at the conclusion that methods based on PSO and BFO intelligent

algorithms are quite efficient in achieving a very good control performance of high order processes and especially high order processes with time delay. Specifically, the resulting rise times  $t_r$  and settling times  $t_s$  are reduced considerably (respectively 6-12 times and 6-15 times), resulting in control systems that have a faster response to changes at the system's input. From Tables

II, III, IV, we conclude that ITSE and ITAE integral criterions, applied as cost functions to find the optimal values of  $K_p$ ,  $K_b$ ,  $K_d$  coefficients of PID controllers are the best functions that can be used for the methods discussed above. From the obtained results, the best integral criterion to be used in the cases of PSO and BFO algorithms is ITSE. Comparing the overall results from the application of the bio-inspired intelligent algorithms, we concluded that the PSO algorithm is more efficient and provides a better tuning of the process than BFO algorithm. It provides less overshoot in the step response of the system in the majority of the cases. Based on the simulations, computing time of PSO algorithm resulted smaller compared to BFO algorithm and this can be justified by the fact that PSO algorithm.







Fig. 8 Best achieved step responses for process  $G_1$  and  $G_2$ .

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