A SVAR approach of the relationship between shadow economy and unemployment rate: The case of United States

Adriana AnaMaria Alexandru, Ion Dobre, Catalin Corneliu Ghinararu

Abstract—The paper analyses the relationship between shadow economy and unemployment rate using a Structural VAR approach for quarterly data during the period 1980-2009. The size of the shadow economy as % of official GDP is estimated using a MIMIC model with four causal variables (taxes on corporate income, contributions for government social insurance, unemployment rate and self-employment) and two indicators (index of real GDP and civilian labour force participation rate). Their dimension is decreasing over the last two periods.

The relationship between the two variables is further tested by imposing a long-run restriction in the Structural VAR model to analyze the impact of the shadow economy to a temporary shock in unemployment. The impulse response function generated by the Structural VAR confirms that in the short-run, a rise in the unemployment rate in formal sector will lead to an increase in the number of people who work in the shadow economy. We extend the classical Okun law, in order to estimate the relationship between growth rate of official economy, unemployment rate and the size of the shadow economy. The results reveal a significant direct relationship between shadow economy and the unemployment rate and an indirect relation between shadow economy and growth of official sector.

Keywords—shadow economy, unemployment rate, MIMIC model, SVAR approach, Okun law.

1. Introduction

The relationship between the shadow economy and the level of unemployment is of major interest. People work in the shadow economy because of the increased cost that firms in the formal sector have to pay to hire a worker. The increased cost comes from the tax burden and government regulations on economic activities. In discussing the growth of the shadow economy, the empirical evidence suggests two important factors: (a) reduction in official working hours, (b) the influence of the unemployment rate.

Enste [20] points out that the reduction of the number of working hours below worker's preferences raises the quantity of hours worked in the shadow economy. Early retirement also increases the quantity of hours worked in the shadow economy.

In Italy, Bertola and Garibaldi [6] present the case that an increase in payroll taxation can have effect on the supply of labour and the size of the shadow economy. An increase in tax and social security burdens not only reduces official employment but tends to increase the shadow labour force. This is because an increase in payroll tax can influence the decision to participate in official employment. Also, Boeri and Garibaldi [8] show a strong positive correlation between average unemployment rate and average shadow employment across 20 Italian regions during the period 1995-1999.

Dell’Anno and Solomon [13] find a positive relationship between unemployment rate and shadow economy, showing that a positive aggregate supply shock will cause in increase in the shadow economy by about 8% above the baseline. The paper analyzes the relationship between SE and UR using a structural VAR approach (SVAR). Also, a reexamination of the classical Okun’s law is provided in the paper, showing the relationship between unemployment and official economy in the presence of shadow economy.

2. Data and Methodology

2.1. Data issues

The variables used in the estimation are defined in appendix A. The data series are quarterly, seasonally adjusted covering the period 1980:Q1 to 2009:Q2. The series in levels or differences have been tested for unit roots using the Augmented Dickey Fuller (ADF) test and PP tests. All the data has been differentiated for the achievement of the stationarity (appendix, unit root analysis). While all the variables have been identified like integrated on first order, the latent variable is estimated in the same transformation of independent variables (first difference).

2.2 Methodology

The size of the U.S. shadow economy is estimated as % of official GDP using a particular type of structural equations models-MIMIC model.

The MIMIC model- Multiple Indicators and Multiple Causes model (MIMIC model), allows to consider the SE as a
“latent” variable linked, on the one hand, to a number of observable indicators (reflecting changes in the size of the SE) and on the other, to a set of observed causal variables, which are regarded as some of the most important determinants of the unreported economic activity [10].

The model is composed by two sorts of equations, the structural one and the measurement equations system. The equation that captures the relationships among the latent variable (η) and the causes (X) is named “structural model” and the equations that links indicators (Y) with the latent variable (non-observed economy) is called the “measurement model”.

A MIMIC model of the hidden economy is formulated mathematically as follows:

\[ Y = \lambda \eta + \varepsilon \]  
\[ \eta = \gamma X + \xi \]

where:
- \( \eta \) is the scalar latent variable (the size of shadow economy);
- \( Y' = (Y_1, ..., Y_p) \) is the vector of indicators of the latent variable;
- \( X' = (X_1, ..., X_q) \) is the vector of causes of \( \eta \);
- \( \lambda', \gamma', \) and \( \xi' \) vectors of parameters;
- \( \varepsilon' \) vectors of scalar random errors;

The \( \varepsilon' \) s and \( \xi' \) are assumed to be mutually uncorrelated. Substituting (2) into (1), the MIMIC model can be written as:

\[ Y = \Pi X + z \]

where: \( \Pi = \lambda \gamma' \), \( z = \lambda \xi' + \varepsilon \).

The estimation of (1) and (2) requires a normalization of the parameters in (1), and a convenient way to achieve this is to constrain one element of \( \lambda \) to some pre-assigned value (1)-(2)).

The possible causes of shadow economy considered in the model are: tax burden decomposed into personal current taxes (\( X_1 \)), taxes on production and imports (\( X_2 \)), taxes on corporate income (\( X_3 \)), contributions for government social insurance (\( X_4 \)) and government unemployment insurance (\( X_5 \)), unemployment rate (\( X_6 \)), self-employment in civilian labour force (\( X_7 \)), government employment in civilian labour force (\( X_8 \)) called bureaucracy index. The indicator variables incorporated in the model are: real gross domestic product index (\( Y_1 \)), currency ratio \( M_1/M_2 (Y_2) \) and civilian labour force participation rate (\( Y_3 \)).

The variables used into the estimation of the shadow economy are also quarterly and seasonally adjusted covering the period 1980-2009. All the data has been differentiated for the achievement of the stationarity.

In order to estimate the MIMIC model, by Maximum Likelihood, using the LISREL 8.8 package, we normalized the coefficient of the index of real GDP (\( \lambda_i = -1 \)) to sufficiently identify the model. This indicates an inverse relationship between the official and shadow economy.

In order to identify the best model, we have started with MIMIC model 8-1-3 and we have removed the variables which have not structural parameters statistically significant.

A detailed description and implementation of the MIMIC model for the USA shadow economy is provided in [17].

After we estimate the size of the shadow economy, we investigate the existence of a structural relationship between shadow economy and unemployment in order to extract information on aggregate supply and aggregate demand disturbances. We use the Structural Vector Autoregression Approach (SVAR) to isolate disturbances as developed by Blanchard and Quah [7].

The structural VAR methodology with long-run restrictions proposed by Blanchard and Quah [7] does not impose restrictions on the short-run dynamics of the permanent component of output, but incorporates a process for permanent shocks that is more general than a random walk. Also, the methodology provides an alternative way to obtain a structural identification. Instead of associating each disturbance (st) directly with an individual variable, they consider the shocks having either temporary or permanent effects. They then treat these shocks like exogenous variables. The objective is to decompose real GNP into its temporary and permanent components. Economic theory is used to associate aggregate demand shocks as being the temporary shocks and aggregate supply shocks as having permanent effects. Using a bivariate VAR, Blanchard and Quah [7] show how to decompose real GNP and recover the two pure shocks that can not otherwise be quantified.

In the same manner, we consider a Vector Autoregression representation of a system composed by two variables that are the first differences of the shadow economy (SE) and unemployment rate (UR). The Blanchard - Quah technique requires that both variables must be stationary.

Thus, the two variables that compose VAR are:

\[ X_1 = \begin{bmatrix} \Delta SE_t \\ \Delta UR_t \end{bmatrix} \]

The classical VAR can be writing as:

\[ \Delta SE_t = b_{10} - b_{11} \Delta UR_t + \gamma_{11} \Delta SE_{t-1} + \gamma_{12} \Delta UR_{t-1} + \ldots + \gamma_{1p} \Delta SE_{t-p} + \gamma_{12p} \Delta UR_{t-p} + \varepsilon_{dt} \]

\[ \Delta UR_t = b_{20} - b_{21} \Delta SE_t + \gamma_{21} \Delta SE_{t-1} + \gamma_{22} \Delta UR_{t-1} + \ldots + \gamma_{22p} \Delta SE_{t-p} + \gamma_{22p} \Delta UR_{t-p} + \varepsilon_{dt} \]

We can re-write the above equations in a matrix form:
Further, matrices of coefficients,
\[
\begin{bmatrix}
1 & b_{12} \\
0 & 1
\end{bmatrix}
\begin{bmatrix}
\Delta SE_t \\
\Delta UR_t
\end{bmatrix} =
\begin{bmatrix}
0 & 0 \\
0 & 0
\end{bmatrix}
\begin{bmatrix}
\Delta SE_{t-1} \\
\Delta UR_{t-1}
\end{bmatrix} + \ldots
\begin{bmatrix}
0 & 0 \\
0 & 0
\end{bmatrix}
\begin{bmatrix}
\Delta SE_{t-p} \\
\Delta UR_{t-p}
\end{bmatrix} + \begin{bmatrix}
\varepsilon_{dt} \\
\varepsilon_{st}
\end{bmatrix}
\]
\[
\begin{bmatrix}
\gamma_{11} & \gamma_{12} \\
\gamma_{21} & \gamma_{22}
\end{bmatrix}
\begin{bmatrix}
\Delta SE_t \\
\Delta UR_t
\end{bmatrix} + \begin{bmatrix}
\gamma_{11} & \gamma_{12} \\
\gamma_{21} & \gamma_{22}
\end{bmatrix}
\begin{bmatrix}
\Delta SE_{t-1} \\
\Delta UR_{t-1}
\end{bmatrix} + \ldots
\begin{bmatrix}
\gamma_{11} & \gamma_{12} \\
\gamma_{21} & \gamma_{22}
\end{bmatrix}
\begin{bmatrix}
\Delta SE_{t-p} \\
\Delta UR_{t-p}
\end{bmatrix} + \begin{bmatrix}
\varepsilon_{dt} \\
\varepsilon_{st}
\end{bmatrix}
\]
(7)

Furthermore, in general form it becomes:
\[
BX_t = \Gamma_0 + \Gamma_1 X_{t-1} + \ldots + \Gamma_p X_{t-p} + \varepsilon_t
\]
(8)

where:
\[
X_t
\]
is a vector of the two considered variables, \(\Gamma_t\) are the matrices of coefficients, \(p\) lags are considered and \(\varepsilon_t\) is the vector of error terms.

By multiplying with the inversion of \(B\) matrix (1 - \(b_{12}b_{21} \neq 0\)) we obtain:
\[
X_t = B^{-1}\Gamma_0 + B^{-1}\Gamma_1 X_{t-1} + \ldots + B^{-1}\Gamma_p X_{t-p} + B^{-1}\varepsilon_t
\]
(9)

Further, \(X_t = A_0 + A_1 X_{t-1} + \ldots + A_p X_{t-p} + \varepsilon_t\)
(10)

\[
X_t = A(L)X_t + \varepsilon_t
\]
(11)

Since the demand-side and supply-side shocks are not observed, the problem is to recover them from a VAR estimation. The critical insight is that VAR residuals are composites of pure innovations \(\varepsilon_{dt}\) and \(\varepsilon_{st}\).

In the particular bivariate moving average form, the VAR can be written:
\[
\begin{bmatrix}
\Delta SE_t \\
\Delta UR_t
\end{bmatrix} = \sum_{i=0}^{\infty} \begin{bmatrix}
0 & b_{12i} \\
0 & 0
\end{bmatrix}
\begin{bmatrix}
\Delta SE_{t-i} \\
\Delta UR_{t-i}
\end{bmatrix} + \begin{bmatrix}
0 & 0 \\
0 & 0
\end{bmatrix}
\begin{bmatrix}
\Delta SE_{t-p} \\
\Delta UR_{t-p}
\end{bmatrix} + \begin{bmatrix}
\varepsilon_{dt} \\
\varepsilon_{st}
\end{bmatrix}
\]
(12)

The vector \(\varepsilon_t = \begin{bmatrix} \varepsilon_{dt} \\ \varepsilon_{st} \end{bmatrix}\) contains the two structural shocks, the demand one and the supply one. The elements \(b_{12i}\) and \(b_{22i}\) are the impulse responses of an aggregate demand shock on the time path of the shadow economy and unemployment rate. The coefficients \(b_{12i}\) and \(b_{22i}\) are the impulse responses of an aggregate supply shock on the time path of shadow economy and unemployment rate respectively.

According to Blanchard and Quah, the key is to assume that one of the structural shocks has a temporary effect on \(\Delta SE\). We assume that an aggregate supply (unemployment rate) shock has no long-run effect on shadow economy. In other words, we impose a long-run restriction on the relationship between the observed data (SE) and the unobserved structural shock \(\varepsilon_{st}\) such that:
\[
\sum_{i=0}^{\infty} b_{12i} = 0
\]
(13)

Equation (13) is an Aggregate Supply Shock stating that the second structural shock (aggregate supply) has no long-run effect on shadow economy.

3. Empirical results

3.1. Estimating the size of the shadow economy

In order to estimate the size of the shadow economy, we have identified the best model as MIMIC 4-1-2 with four causal variables (taxes on corporate income, contributions for government social insurance, unemployment rate and self-employment) and two indicators (index of real GDP and civilian labour force participation rate).

Taking into account the reference variable \(Y_t, Real GDP_{1990}\) the shadow economy is scaled up to a value in 1990, the base year, and we build an average of several estimates from this year for the U.S.A. shadow economy (table 1).

The index of changes of the shadow economy \(\eta\) in United States measured as percentage of GDP in the 1990 is linked to the index of changes of real GDP as follow:
\[
\frac{GDP_{t} - GDP_{t-1}}{GDP_{1990}} = \frac{\eta_t - \eta_{t-1}}{GDP_{1990}}
\]
(14)

I. Estimates of the size of U.S.A. shadow economy (1990)

<table>
<thead>
<tr>
<th>Author</th>
<th>Method</th>
<th>Size of Shadow Economy</th>
</tr>
</thead>
<tbody>
<tr>
<td>Lacko(1999)</td>
<td>Physical Input(Electricity)</td>
<td>10.5%</td>
</tr>
<tr>
<td>Schneider and Enste(2000)</td>
<td>Currency Demand Approach</td>
<td>7.5%*</td>
</tr>
<tr>
<td>Mean 1990</td>
<td></td>
<td>10.6%</td>
</tr>
</tbody>
</table>

*means for 1990-1993

The estimates of the structural model are used to obtain an ordinal time series index for latent variable (shadow economy):

Structural Equation:
\[
\frac{\Delta \bar{\eta}}{GDP_{1990}} = -0.24X_1 + 3.00X_4 + 1.49X_6 + 1.01X_7
\]
(15)
The index is scaled to take up to a value of 10.6% in 1990 and further transformed from changes respect to the GDP in the 1990 to the shadow economy as ratio of current GDP:

\[
\frac{\tilde{\eta}_t}{GDP_{1990}} \times \frac{\tilde{\eta}_{1990}^*}{GDP_{1990}} \times \frac{GDP_{1990}}{GDP_t} = \frac{\hat{\eta}_t}{GDP_t} \quad (16)
\]

I. \( \frac{\tilde{\eta}_t}{GDP_{1990}} \) is the index of shadow economy calculated by (15);

II. \( \frac{\tilde{\eta}_{1990}^*}{GDP_{1990}} = 10.6\% \) is the exogenous estimate of shadow economy;

III. \( \frac{\tilde{\eta}_{1990}}{GDP_{1990}} \) is the value of index estimated by (15);

IV. \( \frac{GDP_{1990}}{GDP_t} \) is to convert the index of changes respect to base year in shadow economy respect to current GDP;

V. \( \frac{\hat{\eta}_t}{GDP_t} \) is the estimated shadow economy as a percentage of official GDP.

Fig. 1. The size of the shadow economy in United States as % of official GDP

The shadow economy measured as percentage of official GDP records the value of 13.41% in the ﬁrst trimester of 1980 and follows an ascendant trend reaching the value of 16.77% in the last trimester of 1982. At the beginning of 1983, the dimension of USA shadow economy begins to decrease in intensity, recording the average value of 6% of GDP at the end of 2007. For the last two year 2008 and 2009, the size of the unreported economy it increases slowly, achieving the value of 7.3% in the second quarter of 2009.

The results are not far from the last empirical studies for USA ([20], [34]). Schneider estimates in his last study, the size of USA shadow economy as % of GDP, at the level of 7.9% in 2005, respectively 8% in 2006.

3.2. There is a link between shadow economy and unemployment rate in the case of United States?

In many empirical studies, it has been found that tax burden is the biggest causes of shadow economy. Also the size of shadow economy is inﬂuenced by the level of unemployment. An increase in unemployment rates reduces the proportion of workers employed in the formal sector this leads to higher labor participation rates in the informal sector.

The graphical evolution of the shadow economy versus unemployment rate reveal the existence of a strong positive relationship between the two variables, quantiﬁed by a value of about 0.80 of correlation coefﬁcient.

Fig. 2. Shadow economy vs. Unemployment rate in United States

Giles ([21], [22]) states that the effect of unemployment on the shadow economy is ambiguous (i.e. both positive and negative). An increase in the number of unemployed increases the number of people who work in the black economy because they have more time. On the other hand, an increase in unemployment implies a decrease in the shadow economy. This is because the unemployment is negatively related to the growth of the official economy (Okun’s law) and the shadow economy tends to rise with the growth of the official economy.

3.2.1. Evaluating the relationship between the shadow economy and the unemployment rate: a SVAR approach

In order to analyze the nature of the relationship between the two variables, we use the Structural VAR approach, for Blanchard and Quah [7] methodology. In order to identify supply and demand shocks, we start by running a bivariate VAR model.

Both variables included in the VAR analysis, are suspected to have a unit root. To verify this, ADF and PP unit
root tests were applied; the results are presented in table II. The size of the shadow economy seems to be stationary in ADF test at level, but this is not justified by PP test. Furthermore, both tests reveal that the variables are non-stationary at their levels but stationary at their first differences, being integrated of order one, I(1).

II. ADF and PP tests for Unit Root analysis

<table>
<thead>
<tr>
<th>Level</th>
<th>Shadow Economy(SE)</th>
<th>Unemployment rate(UR)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>T&amp;C</td>
<td>C</td>
</tr>
<tr>
<td>ADF</td>
<td>-1.09 (3)</td>
<td>-1.39 (6)</td>
</tr>
<tr>
<td>PP</td>
<td>-2.26 (6)</td>
<td>-0.92 (6)</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>First diff</th>
<th>Shadow Economy(SE)</th>
<th>Unemployment rate(UR)</th>
</tr>
</thead>
<tbody>
<tr>
<td>ADF</td>
<td>-3.43* (2)</td>
<td>-3.39** (2)</td>
</tr>
<tr>
<td>PP</td>
<td>-6.59* (3)</td>
<td>-6.57* (3)</td>
</tr>
<tr>
<td>lag</td>
<td>(2)</td>
<td>(2)</td>
</tr>
</tbody>
</table>

Note: T&C represents the most general model with a drift and trend; C is the model with a drift and without trend; None is the most restricted model without a drift and trend. Numbers in brackets are lag lengths used in ADF test (as determined by SCH set to maximum 12) to remove serial correlation in the residuals. When using PP test, numbers in brackets represent Newey-West Bandwith (as determined by Bartlett-Kernel). Both in ADF and PP tests, unit root tests were performed from the most general to the least specific model by eliminating trend and intercept across the models (See Enders, 1995: 254-255). *, ** and *** denote rejection of the null hypothesis at the 1%, 5% and 10% levels respectively. Tests for unit roots have been carried out in E-VIEWS 6.0.

Because the both series are integrated of the same order, I(1) we will difference the variables and we introduce the first difference in the VAR analysis. Including a sufficient number of lags to eliminate serial correlation from the residuals is crucial as using a lag structure that is too parsimonious can significantly bias the estimation of the structural components.

While according to SC and HQ criterions the optimal number of lags is found to be 1, AIC, LR and FPE criterions state that the optimal lag length is 4. Since the usual advice is that when quarterly data are available a minimum length of four is necessary and in order to be sure that through the number of chosen lags the residuals do not remain with autocorrelation, we have selected the optimal number of lags to be 4.

We have estimated a VAR model with four lags who verifies the stability condition\(^1\). Furthermore, we impose on this VAR a long-run restriction which specifies that the long run effect of the supply shocks on the shadow economy is null. Starting from this model, we analyze the impulse response function for the structural version of the model.

\(^1\) Since each VAR represents a system of linear first-order difference equations, it is stable only if the absolute values of all eigenvalues of the system matrix lie inside the unit circle.
3.2.2. A re-examination of Okun’s law in presence of shadow economy

The Okun’s law relates decreases in the unemployment rate to increases in output growth. We want to test if the shadow economy has any significant effect on this empirical evidence. We go on the hypothesis that a lower growth rate of official GDP from potential output is associated with higher deviations of the unemployment rate from its “natural” level. The increase in unemployment leads to an increase in the number of laborers who work in the unofficial labour market.

In fig.1(appendix), we present the significant statistical relationships among growth rate of official GDP, changes in unemployment rate and growth of shadow economy for the case of United States covering the period 1980-2009.

The estimates obtained based on the standard relation given by Okun’s law are presented in the following table:

\[ g_t^Y = \alpha_0 \Delta u_t + \varepsilon_t \]  \hspace{1cm} (17)

where:

\[ g_t^Y = (g_{t}^{off} - \bar{g}^{Y}_{(80-09)}) \] indicates the difference of growth rate of the official gross domestic product \( g_{t}^{off} \) from it average calculated over the period 1970 to 2008;

\[ g_t^n = (g_{t}^{shad} - \bar{g}^{n}_{(80-09)}) \] indicates the difference of shadow economy \( g_{t}^{shad} \) from it average calculated over the period 1980 to 2009, \( \Delta u_t \) id the first difference of unemployment rate, \( \varepsilon_t \) are residuals i.i.d.

III. Estimation output of regression:

\[ g_t^Y = \alpha_0 \Delta u_t + \varepsilon_t \]

IV. Estimation output of regression:

\[ g_t^Y = \alpha_0 \Delta u_t + \beta g_t^n + \varepsilon_t \]  \hspace{1cm} (18)

The econometric results reveal that we have a significant negative relationship on the one hand, between the growth rate of official economy and the level of unemployment, that confirm the Okun’s law, and on the other hand, between the growth rate of official output and the size of the shadow economy. We deduce therefore, that shadow economy tends to cushion the effects of changes in unemployment on the official GDP.

In order to investigate the impact of shadow economy on the unemployment rate, we develop a structural relationship, taking into account also the growth rate of official GDP:

\[ g_t^{shad} = \gamma g_{t}^{off} + \lambda \Delta u_t + \varepsilon_t \]  \hspace{1cm} (19)

where:

\( (g_{t}^{off}) \) is the first difference of annual growth rate of the official gross domestic product;

\( g_t^{shad} \) is the first difference of the shadow economy;

\( \Delta u_t \) is the first difference of unemployment rate; \( \varepsilon_t \) residuals;
V. Estimation output of regression:

\[ g_{t}^{\text{shad}} = c + g_{t}^{\text{off}} + \lambda \Delta u_{t} + \varepsilon_{t} \]

The parameter \( \gamma \) of the equation shows an inverse relationship between the growth of the official economy \( (g_{t}^{\text{off}}) \) and growth of the shadow economy \( (g_{t}^{\text{shad}}) \). On the other hand, the parameter \( \lambda \) shows a direct relationship between changes in unemployment and the growth of the shadow economy.

The coefficients are statistically significant (prob.<5%) and the degree of determination in the model is high, 75% of the variation of shadow economy is explained by the two exogenous variables unemployment rate and growth rate of official GDP.

Our estimations show that the presence of the shadow economy acts as a buffer as it absorbs some of the unemployed workers from the official economy into the shadow economy.

4. Conclusions

In this paper, a structural VAR methodology with long-run restrictions was applied to analyze to relationship between shadow economy and unemployment rate for the case of United States. The size of the shadow economy estimated using the MIMIC model is decreasing over the last two decades, from thirteen to seventeen percent between 1980 and 1983 up to 7% of official GDP at the end of 2009.

The impulse response function generated by the Structural VAR confirms that in the short-run, a rise in the unemployment rate in formal sector will lead to an increase in the number of people who work in the shadow economy.

We extend the classical Okun’s law, in order to estimate the relationship between growth rate of official economy, unemployment rate and the size of the shadow economy.

The results reveal a significant direct relationship between shadow economy and the unemployment rate and an indirect relation between shadow economy and growth of official sector.

Moreover, we can conclude that employment in the shadow economy constitutes a form of labor market transition between or rather from unemployment back into formal employment.

References

## Appendix. Unit-root analysis

The data sources are: Bureau of Economic Analysis (BEA), Bureau of Labor Statistics Data (BLS) and Federal Reserve Banks.

<table>
<thead>
<tr>
<th>CAUSES</th>
<th>Source</th>
<th>Unit root analysis</th>
<th>Level</th>
<th>First Difference</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td>ADF</td>
<td>lag</td>
</tr>
<tr>
<td>X₁ Personal current taxes/GDP</td>
<td>BEA</td>
<td>I(1)</td>
<td>T&amp;C</td>
<td>-2.474</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>C</td>
<td>-2.493</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>None</td>
<td>-0.881</td>
</tr>
<tr>
<td>X₂ Taxes on production and imports/GDP</td>
<td>BEA</td>
<td>I(1)</td>
<td>T&amp;C</td>
<td>-3.543</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>C</td>
<td>-2.922</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>None</td>
<td>0.289</td>
</tr>
<tr>
<td>X₃ Taxes on corporate income/GDP</td>
<td>BEA</td>
<td>I(1)</td>
<td>T&amp;C</td>
<td>-4.19*</td>
</tr>
<tr>
<td></td>
<td></td>
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<td>C</td>
<td>-4.14*</td>
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<tr>
<td></td>
<td></td>
<td></td>
<td>None</td>
<td>-1.18</td>
</tr>
<tr>
<td>X₄ Contributions for government social insurance/GDP</td>
<td>BEA</td>
<td>I(1)</td>
<td>T&amp;C</td>
<td>-2.32</td>
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<td></td>
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<td></td>
<td></td>
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<td>None</td>
<td>0.62</td>
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<td>X₅ Government unemployment insurance</td>
<td>BEA</td>
<td>I(1)</td>
<td>T&amp;C</td>
<td>-2.63</td>
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<td></td>
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<td></td>
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<td>None</td>
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<tr>
<td>X₆ Unemployment rate</td>
<td>BLS</td>
<td>I(1)</td>
<td>T&amp;C</td>
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<td>-0.22</td>
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<td>X₇ Self-employment/Civilian labour force</td>
<td>BLS</td>
<td>I(1)</td>
<td>T&amp;C</td>
<td>-2.44</td>
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<td></td>
<td></td>
<td></td>
<td>C</td>
<td>-0.90</td>
</tr>
<tr>
<td></td>
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<td>None</td>
<td>-0.71</td>
</tr>
<tr>
<td>X₈ Index of bureaucracy</td>
<td>BLS</td>
<td>I(1)</td>
<td>T&amp;C</td>
<td>-2.69</td>
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<td>-2.88</td>
</tr>
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### INDICATORS

| Y₁ M₁ / M₂ | Federal Reserve Banks | I(1) | T&C   | -2.12  | 2    | -1.43  | 8     | -3.02  | 1    | -6.59*  | 7     |
|            |                      |      | C     | -1.69  | 2    | -0.90  | 8     | -3.03* | 1    | -6.51*  | 7     |
|            |                      |      | None  | -0.59  | 2    | -0.78  | 8     | -3.02* | 1    | -6.48*  | 7     |
| Y₂ Index of Real GDP² | BEA   | I(1) | T&C   | -1.71  | 2    | -2.35  | 4     | -5.43* | 1    | -8.71*  | 4     |
|            |                      |      | C     | 1.14   | 2    | 2.03   | 5     | -5.26* | 1    | -8.44*  | 4     |
|            |                      |      | None  | 4.63   | 2    | 9.68   | 5     | -2.39* | 1    | -4.45*  | 6     |
| Y₃ Civilian labor force participation rate | BLS    | I(1) | T&C   | -0.47  | 2    | -0.66  | 1     | -10.29* | 1  | -10.59* | 0     |
|            |                      |      | C     | -2.03  | 0    | -2.08  | 3     | -5.98* | 2    | -10.08* | 4     |
|            |                      |      | None  | 1.12   | 0    | 1.15   | 4     | -5.81* | 2    | -10.01* | 5     |

| Y₂ Index of Real GDP² | BEA   | I(1) | T&C   | -1.71  | 2    | -2.35  | 4     | -5.43* | 1    | -8.71*  | 4     |
|                      |       |      | C     | 1.14   | 2    | 2.03   | 5     | -5.26* | 1    | -8.44*  | 4     |
|                      |       |      | None  | 4.63   | 2    | 9.68   | 5     | -2.39* | 1    | -4.45*  | 6     |

Note:
T&C represents the most general model with a drift and trend; C is the model with a drift and without trend; None is the most restricted model without a drift and trend. Numbers in brackets are lag lengths used in ADF test (as determined by SCH set to maximum 12) to remove serial correlation in the residuals. When using PP test, numbers in brackets represent Newey-West Bandwith (as determined by Bartlett Kernel). Both in ADF and PP tests, unit root tests were performed from the most general to the least specific model by eliminating trend and intercept across the models (Katircioglu, 2009). *, ** and *** denote rejection of the null hypothesis at the 1%, 5% and 10% levels respectively. Tests for unit roots have been carried out in E-VIEWS 6.0.

![Graph 1](image1)

**Fig.1.** Growth of official GDP, Changes in unemployment and Growth of Shadow Economy