

# FPGA Implementation of Ternary Pulse Compression Sequences with Superior Merit Factors

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**Abstract**— Ternary codes have been widely used in radar and communication areas, but the synthesis of ternary codes with good merit factor is a nonlinear multivariable optimization problem, which is usually difficult to tackle. To get the solution of above problem many global optimization algorithms like genetic algorithm, simulated annealing, and tunneling algorithm were reported in the literature. However, there is no guarantee to get global optimum point. In this paper, a novel and efficient VLSI architecture is proposed to design Ternary Pulse compression sequences with good Merit factor. The VLSI architecture is implemented on the Field Programmable Gate Array (FPGA) as it provides the flexibility of reconfigurability and reprogramability. The implemented architecture overcomes the drawbacks of non guaranteed convergence of the earlier optimization algorithms.

**Keywords**— FPGA, Pulse compression, Ternary sequence, VLSI architecture.

## I. INTRODUCTION

Pulse compression codes with low autocorrelation sidelobe levels and high merit factor are useful for radar [1], channel estimation, and spread spectrum communication applications. Pulse compression can be defined as a technique that allows the radar to utilize a long pulse to achieve large radiated energy but simultaneously obtaining the range- resolution of a short pulse. Theoretically, in pulse compression, the code is modulated onto the pulsed waveform during transmission. At the receiver, the code is used to combine the signal to achieve a high range resolution. Range-resolution is the ability of the radar receiver to identify near by targets.

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The main criterion of good pulse compression is the Meritfactor and discrimination. Merit factor is used to measure whether coded signal is a good or poor. This means that a code with high Merit factor is a good code while a code with low Merit factor is a poor code. Let

$$S = [x_0, x_1, x_2, x_3, \dots, x_{N-1}] \quad (1)$$

be a real sequence of length N.

The aperiodic autocorrelation function (ACF) of sequence S of length N is given as,

$$A(k) = \begin{cases} \sum_{n=0}^{N-k-1} s_n s_{n+k}^* & ; 0 \leq k \leq N-1 \\ \sum_{n=0}^{N+k-1} s_n s_{n-k}^* & ; -N+1 \leq k \leq 0 \end{cases} \quad (2)$$

## II. MERIT FACTOR (MF)

Golay [2] defined the merit factor (MF) as the ratio of mainlobe energy to sidelobes energy of Autocorrelation (AC) function of sequence S. The MF mathematically is defined as

$$MF = \frac{A(0)^2}{2 \sum_{k \neq 0} |A(k)|^2} \quad (3)$$

The denominator term represents the energy in the sidelobes. The merit factor MF must be as large as possible for good sequence.

## III. NON BINARY PULSE COMPRESSION CODES.

### A. Polyphase Code

Waveforms consisting more than two phases are called polyphase codes. The phase of sub pulse alternate among multiple values rather than  $0^0$  and  $180^0$ . The sequence can be written as

$$\phi_n = \frac{2\pi i(n-1)}{p^2} \quad (4)$$

Where  $p$  is the number of phases,  $n=0, 1, 2, \dots, p^2-1$  and  $i=n$  modulo  $p$

### B. Ternary Code

Ternary Code is the code that can be used to represent information and data. However ternary code uses 3 digits for representation of data. Therefore ternary code may also be called as 3-alphabet code. This code consists of 1, 0, and -1.

## IV. NEED FOR THE PROPOSED ARCHITECTURE

The problem of obtaining long sequences with peaky autocorrelation [3] has long been an important problem in the field of radar, sonar and system identification. It is viewed as the problem of optimization [4-5]. The signal design problem for radar application is suggested by sequences like binary, Polyphase, ternary and Quinquenary sequences. There has been extensive work on ternary sequences for obtaining good Meritfactor values [6-10]. This work was based on global optimization techniques such as genetic algorithm, eugenic algorithm and SKH (Simon-Kronecker-Hamming) algorithm. But all these optimization algorithms have serious drawbacks of non guaranteed convergence, slow convergence rate and require large number of evaluations of the objective function. The Hardware Implementation architectures for Pulse compression signal processing systems available in the literature have the capability of only the generation of pulse compression sequences with limited speed [11-12]. Hence earlier the authors proposed an efficient VLSI architecture for the generation of the Pulse Compression sequences with FPGA clock rate [13-16].

The proposed architecture shown in Fig.1 is a single chip solution for the identification of good Ternary pulse compression sequences. Hardly any integrated hardware architecture was available in the literature with the identification and generation of ternary pulse compression sequence capabilities. The architecture shown in Fig.1 was tested on a single FPGA. With a little additional hardware, the proposed architecture can generate good Ternary Pulse Compression sequences with FPGA clock rate. Hence in this paper we proposed an efficient real time Hardware solution for identification of the Ternary Pulse compression sequences.

## V. PROPOSED ARCHITECTURE

As the main lobe energy  $A^2(0)$  of a given Ternary sequence of length  $N$  is  $N^2$  from equation 3, for the merit factor calculation of a Ternary sequence, we need to calculate the side lobe energy of a Ternary sequence. Since Meritfactor is the main criterion for good pulse compression sequences, therefore the Ternary sequence having minimum sidelobe energy can be considered as the best Ternary Pulse compression sequence. The proposed VLSI architecture for identification of the good ternary pulse compression is shown in the Fig. 1. The

architecture mainly consists of eight blocks. They are sequence generator, sign conversion unit, multiplexer, multiplier, adder and accumulator unit, squaring unit, series of adder circuits, comparator and registers. The sequence generator is a synchronous counter. The counter consists of two inputs preset and clock. At the beginning of counter operation the preset is set to one and it is bring back to zero. The architecture generates  $3^N$  Ternary sequences of length  $N$ . For all these  $3^N$  sequences it calculates the sidelobe energy values, identifies and holds the sequence with minimum sidelobe energy. The sequence generator is a synchronous counter of length  $N$  which generates  $3N$  sequences with 0's and 1's. These generated sequences are modified with the help of the sign conversion unit to get the Ternary Pulse Compression sequence elements. As the ternary sequence consists of 0, +1 and -1, the sign conversion unit converts the bit '1' to 01, '0' to 00 and '-1' to 11. The multiplexer unit consists of inputs, select lines. The output of counter block is given as select lines to the multiplexer. Depending on the combinations of the select lines, the corresponding input is given to the output. The outputs of multiplexer units are applied as inputs to multiplier units. The remaining hardware blocks are useful for computing, identifying and holding the lowest side lobe energy value of a Ternary pulse compression sequence. The output register2 of Fig. 1 holds the good ternary pulse compression sequence. This sequence is represented by +1's, -1's and 0's. To convert this representation of the sequence to pure ternary sequences of 0, +1 and -1 we need to interface a little additional hardware to FPGA. For lower sequence length the proposed architecture generate all the  $3N$  sequences, identifies and holds the best ternary sequence among the  $3N$  sequences. In order to reduce the computing time and complexity for larger sequences of length  $N$ , the sequence generator of Fig. 1 can be modified to generate  $k$  bits dynamically and remaining  $(N-k)$  bits will be the fixed bits which can be taken from an already identified best sequence of length  $(N-k)$ .

## VI. TECHNOLOGY AND TOOLS

The architecture shown in Fig. 1 has been authored in VHDL for 23-bit and 31-bit Ternary Pulse compression sequences and its synthesis was done with Xilinx XST. Xilinx ISE Foundation 9.1i has been used for performing mapping, placing and routing. For Behavioral simulation and Place and route simulation Modelsim 6.0 has been used. The Synthesis tool was configured to optimize for area and high effort considerations. The targeted device was Spartan-3 xa3s1500fpg676-4 with detailed specifications at [17]. The good 23-bit and 31-bit Ternary Pulse compression sequences implementation reports presented in Table I and Table II respectively.

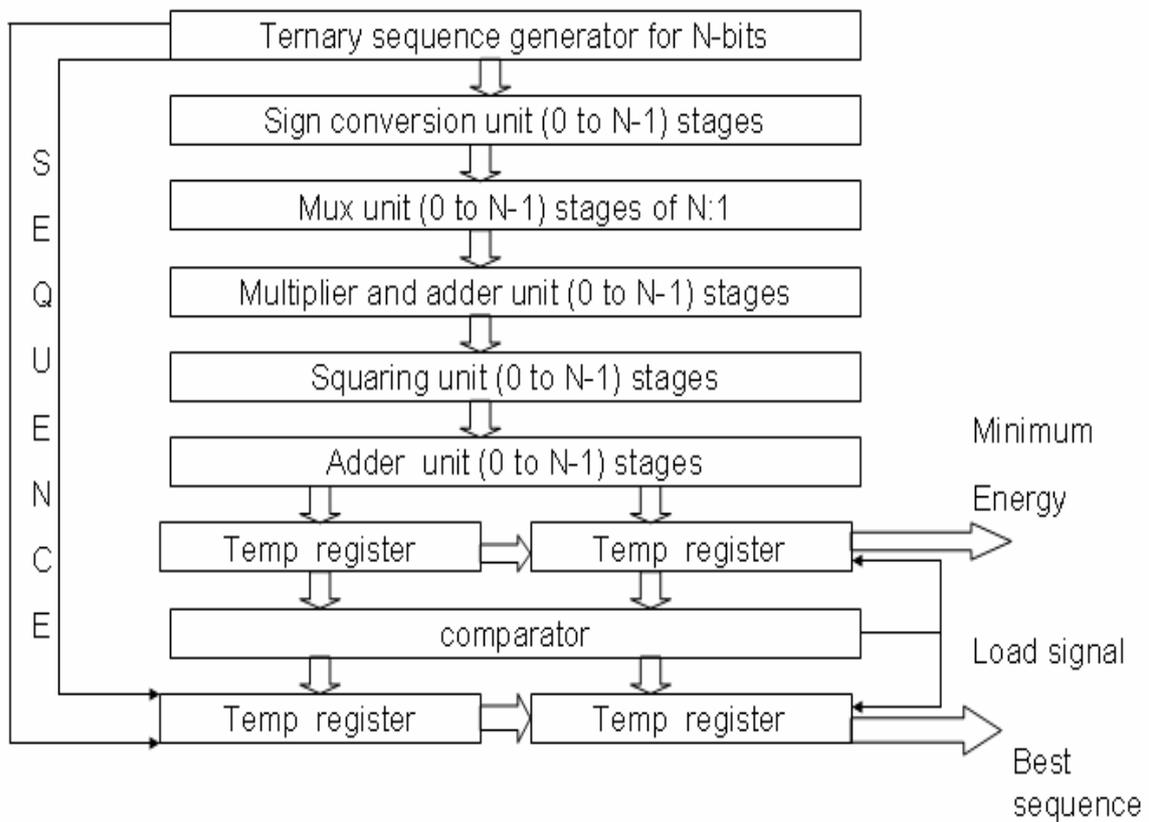


Fig.1. VLSI architecture for the identification of good Ternary pulse compression sequence.

Table I Design Implementation summary of the good 23-bit length Ternary Pulse Compression sequence

<b>Design Summary:</b>		
Number of errors:	0	
<b>Logic Utilization:</b>		
Total Number Slice Registers:	869 out of 66,560	1%
Number used as Flip Flops:	280	
Number used as Latches:	589	
Number of 4 input LUTs:	1,711 out of 66,560	2%
<b>Logic Distribution:</b>		
Number of occupied Slices:	1,453 out of 33,280	4%
Number of Slices containing only related logic:	1,453 out of 1,453	100%
Number of Slices containing unrelated logic:	0 out of 1,453	0%
Total Number of 4 input LUTs:	1,825 out of 66,560	2%
Number used as logic:	1,711	
Number used as a route-thru:	114	
Number of bonded IOBs:	66 out of 784	8%
IOB Latches:	51	
Number of MULT18X18s:	22 out of 104	21%
Number of GCLKs:	3 out of 8	37%
Total equivalent gate count for design:	107,015	
Additional JTAG gate count for IOBs:	3,168	
<b>Timing Summary:</b>		
Minimum period:	5.442ns (Maximum Frequency: 183.746MHz)	
Maximum output required time after clock:	6.141ns	

Table II Design Implementation summary of the good 31-bit length Ternary Pulse Compression sequence.

Design Summary:		
Number of errors:	0	
Logic Utilization:		
Total Number Slice Registers:	1,164 out of 66,560	1%
Number used as Flip Flops:	378	
Number used as Latches:	786	
Number of 4 input LUTs:	2,415 out of 66,560	3%
Logic Distribution:		
Number of occupied Slices:	2,217 out of 33,280	6%
Number of Slices containing only related logic:	2,217 out of 2,217	100%
Number of Slices containing unrelated logic:	0 out of 2,217	0%
Total Number of 4 input LUTs:	2,677 out of 66,560	4%
Number used as logic:	2,415	
Number used as a route-thru:	262	
Number of bonded IOBs:	82 out of 784	10%
IOB Latches:	53	
Number of MULT18X18s:	30 out of 104	28%
Number of GCLKs:	3 out of 8	37%
Total equivalent gate count for design:	147,682	
Additional JTAG gate count for IOBs:	3,936	
Timing Summary:		
Minimum period:	5.442ns (Maximum Frequency: 183.746MHz)	
Maximum output required time after clock:	6.141ns	

From the device utilization Summary the same Spartan-3 FPGA is useful for the implementation of higher lengths of the Ternary Pulse Compression sequence. The behavioral simulation waveforms for the good 23-bit ternary Pulse compression sequence are shown in Fig. 2. The behavioral simulation waveforms for the good 31-bit ternary Pulse compression sequence are shown in Fig. 3. From Fig. 2 it can be seen that ternary sequence based on the lowest sidelobe energy is 011101110100110100110101111000101001111111111000011001101011(-1-1-1-1-10110-1-111-101-101-11-1) and its sidelobe energy is 18. Therefore meritfactor of this sequence is 20.0556. From Fig. 3 it is seen that Ternary sequence based on the lowest sidelobe energy is 01000000011111101111110101010111000001000101110100110 100001(10 0 1 -10 1 -1 1 10 10 0 -1 1 1 1 1 -1 -1 1 1 -1 -1 -1 0 0 0 1) and its sidelobe energy is 30. Therefore meritfactor of this sequence is 16.13333. The generated good Ternary Pulse Compression Sequences for the identified good Ternary Pulse Compression Sequences for the Fig. 2 is shown in Fig. 4. The generated good Ternary Pulse Compression Sequences for the identified good Ternary Pulse Compression Sequences for the Fig. 3 is shown in Fig. 5. Fig. 6 shows the RTL schematic of the proposed architecture that was obtained with the aid of the ISE 9.1i. Fig. 7 shows the Pinout and Area Constraints Editor Diagram. The power analysis was made using Xilinx ISE software version 9.1. The Power analysis summary was presented in Table III.

Table III. Xilinx ISE power consumption summary.

Power summary:	I(mA)	P(mW)
Total estimated power consumption:	319	
Clocks:	10	12
Inputs:	1	2
Logic:	16	40
Outputs:		
Vcco25	30	90
Signals:	70	175

## VII. DESIGN RESULTS

Ternary sequences are designed using the proposed novel and efficient VLSI architecture. In this paper all the synthesized results are single realizations obtained using Spartan-3 FPGA. The use of the FPGA technology was chosen due to it provides some important advantages over general purpose processors and Application Specific Integrated Circuits (ASICs) such as: 1) FPGAs provide massive parallel structures and high density logic arithmetic with short design cycles compared to ASICs, 2) In FPGA devices, tasks are implemented by spatially composing primitive operators rather than temporally, 3) In FPGAs, it is possible to control operations at bit level to build specialized data-paths. Some of the synthesized Ternary sequences, with good Merit Factors are presented. The synthesized sequences have Merit factor better than sequences reported in the literature [10].

BEHAVIORAL SIMULATION RESULTS OF 23 BIT TERNARY PULSE COMPRESSION WAVEFORM

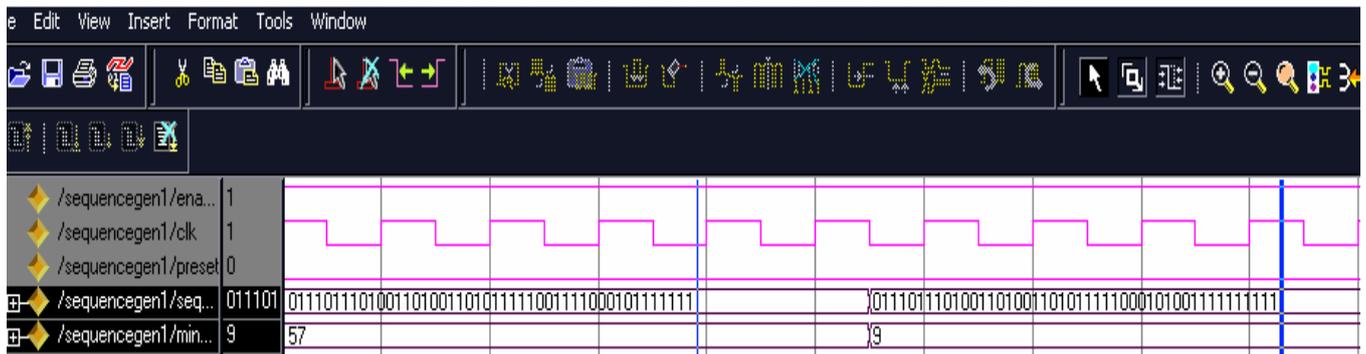


Fig. 2 Behavioral simulation result of a good 23-bit Ternary Pulse compression sequence.

BEHAVIORAL SIMULATION RESULTS OF 31 BIT TERNARY PULSE COMPRESSION WAVEFORM



Fig. 3 Behavioral simulation result of a good 31-bit Ternary Pulse compression sequence.

Generated Ternary Waveform for the Alphabets '0', '+1' and '-1'

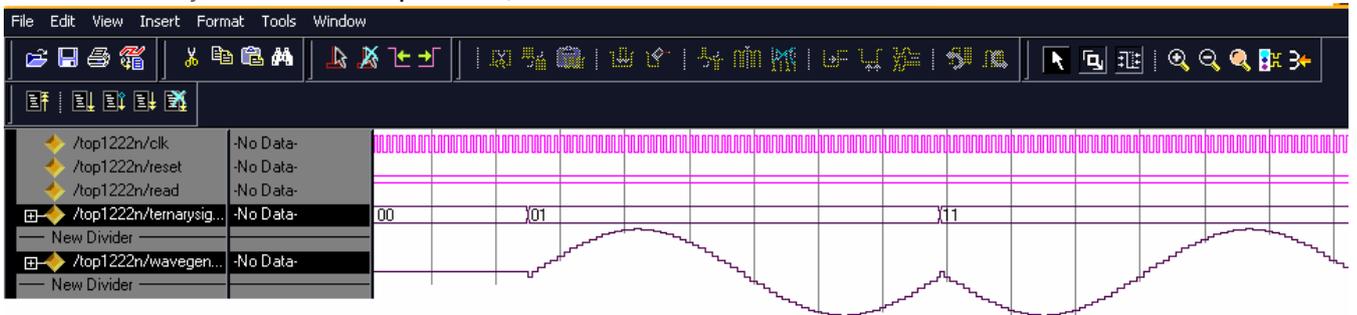


Fig. 4 Generated Ternary Pulse Compression Sequence with the Alphabets '0', '+1' and '-1'

Generated Ternary Sequence Waveform with the alphabets '+1', '-1' and '+1'

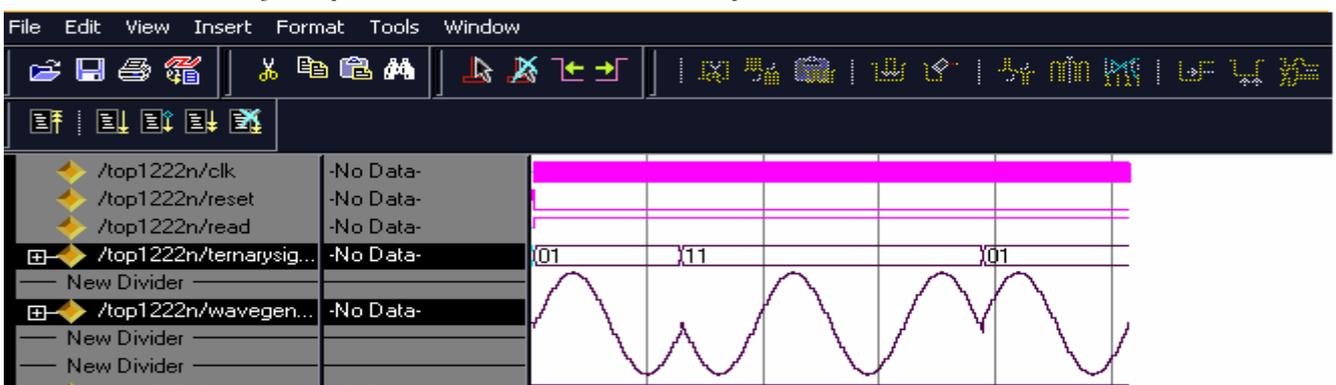


Fig. 5 Generated Ternary Pulse Compression Sequence with the Alphabets '+1', '-1' and '+1'



2, shows Merit Factor (MF). Fig. 8 shows comparison of merit factors of synthesized sequences and sequences reported in the literature [10].

Table IV Merit factor of synthesized Ternary sequences

Sequence Length (1)	MF (2)
21	14.083
31	16.1333
37	10.4651
39	10.5125
41	10.6778
43	13.5000
51	14.0083
61	10.6869
63	8.2034
65	10.8679
67	8.69
69	10.4727
71	10.9136
73	9.8908
75	10.9764
77	8.6429
81	9.7225
83	10.5000
85	11.0860
87	10.2824
89	10.7037
93	8.125
97	9.7438
101	11.956

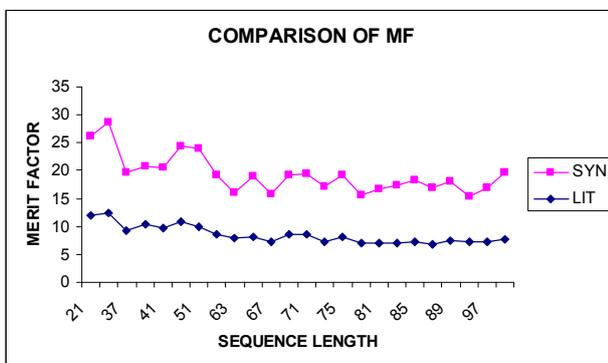


Fig. 8 Comparison of merit factors of synthesized and literature sequences

An efficient VLSI architecture was proposed and implemented for the design of Ternary sequences used in radar and communication systems for significantly

improving the system performance. The synthesized Ternary sequences have good Merit Factors. The synthesized Ternary sequences are promising for practical application to radars and communications. It was also observed that the proposed architecture is giving good Merit Factor values for higher lengths. This shows the superiority of the architecture.

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