

applied, and matrix algebra was utilized, in such a manner that the unknown function was found by solving a linear algebraic equation in a matrix form. The advantage of this method is an inevitable result of adapting a matrix-based algebra technique, where we were able to obtain a monomial basis matrix that facilitated the solution, reduced the steps of the solution and led to its superior accuracy compared with the other methods.

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