

$$c_j = -h(-8\cos(h) + 16\cos^2(h) + 6h\sin(h)\cos(h) + 6h\sin(h) - 8)/(4(h\cos^2(h) - 3\sin(h)\cos(h) + h\cos(h) - 2h + 3\sin(h))),$$

$$c_{j+1} = -h(4\cos(h) + \cos^2(h) + 3h\sin(h) - 5)/(4(h\cos^2(h) - 3\sin(h)\cos(h) + h\cos(h) - 2h + 3\sin(h))),$$

$$c_{j-1} = -h(4\cos(h) + \cos^2(h) + 3h\sin(h) - 5)/(4(h\cos^2(h) - 3\sin(h)\cos(h) + h\cos(h) - 2h + 3\sin(h))).$$

Table 5 shows the actual errors of the smooth polynomial and non-polynomial approximations, $h = 0.4, [a, b] = [-1, 1]$.

Table 5. The actual errors of the smooth polynomial and non-polynomial approximations, $h = 0.4, [a, b] = [-1, 1]$.

Function $u(x)$	Polynomial splines	Non-polynomial splines
$\sin(3x)$	$0.772 \cdot 10^{-4}$	$0.387 \cdot 10^{-4}$
$\sin(7x) - \cos(9x)$	$0.249 \cdot 10^{-1}$	$0.236 \cdot 10^{-1}$
$x^7 - x^9$	$0.110 \cdot 10^{-2}$	$0.121 \cdot 10^{-2}$
$1/(1 + 25x^2)$	$0.358 \cdot 10^{-1}$	$0.361 \cdot 10^{-1}$

REFERENCES

[1] S.G.Mikhlin. "Variational-difference approximation," *J. Math. Sci.*, Vol.10, 1978, pp. 661-787.

[2] E.L.Hart, V.S. Hudramovich, "Application of the Projection-Iterative Scheme of the Method of Local Variations to Solving Stability Problems for Thin-Walled Shell Structures Under Localized Actions," *Strength of Materials*, 50 (6), 2018, pp. 852-858.

[3] R.Pasichnyk, O.Pasichnyk, O.Uzhegova, O.Andriichuk, O. Bondarskii, "Calculation optimization of complex shape shells by numerical method," *Lecture Notes in Mechanical Engineering*, 2020 pp. 643-652.

[4] M.N.Suardi, N.Z.F.M.Radzuan, J.Sulaiman, "Performance of quarter-sweep SOR iteration with cubic B-spline scheme for solving two-point boundary value problems," *Journal of Engineering and Applied Sciences*, 14 (3), 2019, pp. 693-700.

[5] M.Kang, J.Yang, X.Wang, X.Chen, "Study on the variational-difference-based design and slow tool servo turning of progressive addition lenses," *Advances in Mechanical Engineering*, 2018,10(12).

[6] M.S.Korytov, V.S.Shcherbakov, V.V.Titenko, "Application of Hermite splines for load movement on a flexible crane suspension through a curvilinear trajectory," *Journal of Physics: Conference Series*, 1441 (1), paper № 012101, 2020.

[7] Y.K.Dem'Yanovich, O.V. Belyakova, B.T.N.Le, "Uniqueness of Space of Hermite Type Splines," *Proceedings 2018 International Conference on Applied Mathematics and Computational Science, ICAMCS.NET 2018*, paper № 8955759, 2018, pp. 178-183.

[8] E.B. Chin, N.Sukumar, "Modeling curved interfaces without element-partitioning in the extended finite element method," *International Journal for Numerical Methods in Engineering*, vol. 120, no.5, 2019, pp. 607-649.

[9] N.C. Gabrieldes, N.S. Sapidis, "Cubic polynomial and cubic rational C 1 sign,monotonicity and convexity preserving Hermite interpolation," *Journal of Computational and Applied Mathematics*, vol. 357, 2019, pp. 184-203.

[10] I.J.Schoenberg, "On trigonometric spline interpolation," *J Math Mech.*, 13, 1964, pp. 795--825.

[11] Irina Burova, "On left integro-differential splines and Cauchy problem," *International Journal of Mathematical Models and Methods in Applied Sciences*, Vol. 9, 2015, pp. 683-690.

[12] I.G.Burova, "On trigonometric splines construction," *Vestnik Sankt-Peterburgskogo Universiteta, Ser. I. Matematika Mekhanika Astronomiya*, 2, 2004, pp. 9-14.

[13] I.G.Burova, T.O.Evdokimova, "On the smooth second order trigonometric splines," *Vestnik Sankt-Peterburgskogo Universiteta. Ser. I. Matematika Mekhanika Astronomiya*, 3, 2004, pp. 11--16.

[14] I.G. Burova, E.F. Muzafarova, I.I. Narbutovskikh, "Approximation by the Third-Order Splines on Uniform and Non-uniform Grids and Image Processing," *WSEAS Transactions on Mathematics*, Vol. 19, 2020, pp. 65-73.

[15] I. G. Burova, E. F. Muzafarova, "Interval Estimation using Integro-Differential Splines of the Third Order of Approximation," *WSEAS Transactions on Mathematics*, Vol. 18, 2019, pp. 153-160.