Abstract— Performance of any system is identified through the observation of significant system parameters. Required parameters have to be measured using suitable sensors. But in some scenarios, it is difficult to measure some of the parameters due to issues in the placement of sensors. In such cases, estimators are developed to measure the parameters indirectly. In this paper, an attempt is made to develop an estimator to monitor the value of pitch and yaw of a twin-rotor multi input multi output system. The observer is developed using two methods one using Luenberger’s equations and the other using an Artificial Neural Network (ANN). For training the neural network model, the backpropagation algorithm is used. Tests have been conducted to analyze and compare the behavior of both observers. From the results, it is evident that a Luenberger observer performs better when sufficient system information is available and ANN observer performs better when inadequate system information is available.

Keywords—Artificial Neural Network, Estimator, Observer, soft sensor, TMRS.

I. INTRODUCTION

Invention of helicopters were considered as the evolutionary step towards vertical lift vehicles. Study of helicopter system is vital in many ways to understand the behavior of aircrafts. Since, design and implementation of the helicopter will not be viable solutions for many institutes, a TRMS as shown in Figure 1 is implemented to mimic the operation of the same. Several researchers have reported works on understanding this vital component of an aircraft system.

A lot of work have been reported for measurement and control of a TRMS system like in [1], a technique is reported for control of pitch channel in a TRMS using nonlinear inversion control model programmed using ANN and genetic algorithms. Design of a neural Proportional+ Integral+ Differentiator (PID) controller for control of pitch and yaw in TRMS was developed in [2]. PID controller was tuned using real value genetic algorithm. Paper [3] discusses the design of controller for stabilizing the TRMS using a radial basis function neural network algorithm. In [4], a setup is implemented for virtual and remote control practices in a three Degree of Freedom (DOF) quadrotor. TwinCAT Programmable Logic Controller (PLC) are used as the controllers and applet as remote laboratory front-end. Paper [5] discusses a robust tracking system developed using an integral sliding mode controller for a TRMS. Simultaneous estimation of system fault and sensor fault is discussed in [6]. The method discussed reduces the exogenous disturbances to a predefined level apart from the ability to perform simultaneous estimation. Paper [7] explored the concept of shifting linear quadratic control which considered the existence of constraints in the system. Two constraints namely, algebraic constraints between variables of the system and constraints depending on the input and state variables were considered. In [8], a hybrid controller containing a second order data driven Model Free Control (MFC) and Takagi-Sugeno Fuzzy (TSF) logic controller for nonlinear Multi Input-Multi Output twin rotor aerodynamic systems was reported.

A comparison of the performance of the Control System Structure (CSS) using the second order MFC-TSF controller and CSS using the MFC controller was performed. Paper [9] discusses the Integral Quadratic Constraints (IQC) approach, for effective systematic analysis of robust stability. To make IQC analysis tools easily accessible, an overview of three measures namely (i) general setup and basic IQC theorem, (ii) a survey of multipliers based on the linear matrix inequality constraints and (iii) an explanation on application of the tools is done. An analytical method for based on Bode’s ideal transfer function for tuning the parameters of fractional order PI controllers (FOPI) is discussed in [10]. In [10], to attain the closed loop transfer function the factors of the FOPI controller
were tuned. It was found that for low and medium frequency ranges, the robustness of the system is better in FOPID controller with compared to the PI controller with similar configuration.

Paper [11] reports a design and experimental of robust controller for multi input multi output plants. External disturbances and parametric uncertainties were the factors considered for measuring the quantized output. A control strategy for TRMS is discussed in [12], to reach preferred positions in two degrees of freedom, a control strategy built on the coupling of a fuzzy logic control using sliding mode controller. In [13], identification, modeling and control of TRMS for a quasi linear parameter is reported. Nonlinear model is converted in to a quasi LPV system. Paper [14] reported a different nonlinear internal model control approach. The performance and robustness can be improved by varying the control based on flatness property. This enables the model to work in a closed loop structure. Two nonlinear model predictive control algorithms are projected in [15] based on neural networks intensified reactors. One control algorithm is by means of nonlinear-optimization and the other using local linearization.

Paper [16], reports a multi variable nonlinear control oriented model for a twin rotor aerodynamic system. Using Lagrange’s equations, a mathematical description for a multibody system is derived. A multi-variable integral sliding mode control using the resulting state-space representation is designed which tracks the preferred trajectories for azimuth angle and pitch angle. Paper [17] describes data-driven techniques which are applied on a single MIMO controller and two separately designed single-input-single-output controllers. The data driven techniques projected are model-free adaptive control, model-free control and virtual reference feedback tuning techniques. A model predictive control strategy designed for drinking water networks is discussed in [18] which considers the system and component reliability. In [19], an observer centered control method for a two input two output plant is reported. The plant is affected by lumped disturbance which consists of undesired effect of cross couplings, parametric uncertainties and external disturbances.

Paper [20] discusses the development of a model predictive control approach built on a neural network Wiener model. The paper also discusses its application on an intensified continuous reactor. The Wiener model can be grouped into two parts: a linear state space identified model and a local linearization of a neural network model. A laboratory model of a Twin Rotor MIMO system is described in [21] which was created by Feedback Instruments Ltd. The system which looks like a helicopter is made up of two rotors. In [22], a model of the Mamdani type fuzzy two input, two output proportional integral or proportional differentiator controller is reported. The fuzzy controller consists of two fuzzy sets for each input variables, five fuzzy set for each output variable, five linear control rules, AND operator, OR operator and height defuzzification strategy. Paper [23] talks about two model free sliding mode control structures. On comparison with a model free intelligent proportional integral control system structure in regard to performance improved performance is found. Paper [24] describes the design of passivity-based controllers which makes use of memristor. Making use of the passive property of memristor incorporated in the target dynamics. In [25], a linear parameter varying model is reported meant for fixed-wing unmanned aerial vehicles. The objects obtained includes its agility and high performance.

From the literature survey it is clear that a lot of study is reported on TRMS systems, with the focus mainly on the control aspect. A few literature also reports design of sensing technique for measurement of variables like pitch, yaw and roll. Few literature have also focused on the fault tolerant control system, the proposed work makes an attempt to design estimator to measure parameters like pitch yaw in TRMS under the condition of faulty sensors.

The work is organized such that the background study is carried out in first section followed by description of the practical system in Section-II. Section-III reports the methodology of the proposed work. Section-IV discusses the results obtained by the ANN based and observer based techniques. Finally, Section-V discusses the conclusion of the work.

II. SYSTEM DESCRIPTION

Twin rotor multi input and multi output system from feedback instrument Pvt Ltd is used for carrying the experiment in the proposed work. Schematic of the proposed system is shown in Figure 1 [26], the TRMS model similar to the helicopter model. The experimental model consists of beam pivoting on its base at both of its end. The beam is connected with two propeller which are driven by two DC motors. The beam is fabricated in a way such that the beam can traverse in a circular pattern along the axis. A counter weight is provided at the center, to keep the system in the state of equilibrium. The system is designed in a way such that when motors are switched off the end with main rotor in lowered.

![Fig. 1 Schematic of the proposed system](image)

Supply voltage of 230 V AC is used to drive the motor to so
as to control the TRMS parameters. Position angles and angular velocity of the rotor are the two signals which are measured. Software codes are used to reconstruct the angular velocities from the position angles of the beam by differentiation and filtering. Fixed angle of attack of a rotor and aerodynamics are controlled by varying speed of the motor. Cross coupling is observed in the movement of the rotors, with each rotor affecting both angle positions. The two propellers are driven by DC motors and control of the system are the supply voltages for the motor. Measured signals are positioned in the beam in the space that is two position angles which are measured by rotary optical encoders, mounted on each of the rotor shaft. The optical encoder to measure the rotation of the rotor is of incremental type. Figure 2 shows the laboratory model used in the proposed work.

![Image](Fig. 2 TRMS Model from Feedback Instruments)

Instrument specifications
Line voltage: 230 V @ 50 Hz
Consumption: 100 VA.
Weight and Dimensions: 80 cm x 35 cm x 75 cm
Weight: 11 kg.

The objectives of the proposed project work are as follows:

a. To Estimate the Pitch and Yaw angular positions from the noisy and distorted sensor data obtained from the two optical encoders of the tail and main rotors of the TRMS.

b. Secondary objective is to come up with a comparative study of the various estimation algorithms, in terms of error functions: Integral of Absolute Error (IAE), Integral of Square of Error (ISE) and Integral of Absolute Time Error (IATE).

III. PROBLEM SOLUTION

The noisy sensor data obtained from the optical sensors of the two rotors are obtained as the input to the estimation block. This initial value of the sensor outputs as well as the control input is used to estimate the next pitch and yaw angles with an appropriate system model. The reference model is used to give the nominal outputs as shown in Figure 3. The first phase of achieving the objective mentioned is by designing estimators for the TRMS model. In the proposed work two different techniques are used for the same. Firstly a model based technique of observer based estimator is designed and later an ANN based estimator is designed.

A. Luenberger Estimator

The modeling of the system is done using two separate state space representation, one is the pitch model and the other is yaw model. The state space representation of the TRMS system is given by:

\[
\dot{x} = Ax + Bu; \quad y = Cx + Du
\]

(1)

The matrices for Pitch Model:

\[
A = \begin{pmatrix}
-1.4389 & -3.1862 & 1.6706 \\
0.0803 & -4.9874 & -29.1821 \\
-0.0376 & 0.0474 & -5.5737
\end{pmatrix}; \quad B = \begin{pmatrix}
1 \\
0 \\
0
\end{pmatrix};
\]

(2)

\[
C = \begin{pmatrix}
0.0166 & 0.4194 & 2.454
\end{pmatrix}; \quad D=0
\]

The matrices for Yaw Model:

\[
A = \begin{pmatrix}
-1.38 & -1.6456 & -14.7611 \\
0.9244 & -2.5724 & -31.1124 \\
-0.0196 & 0.3346 & -8.0476
\end{pmatrix}; \quad B = \begin{pmatrix}
1 \\
0 \\
0
\end{pmatrix};
\]

(3)

\[
C = \begin{pmatrix}
0.001 & 0.0336 & 0.4065
\end{pmatrix}; \quad D=0
\]

The system equation is given as given by equation (1)

The observer equation is given by:

\[
\dot{\hat{x}} = A\hat{x} + Bu + L \ast (y - \hat{y})
\]

(4)

\[
\dot{\hat{x}} = A\hat{x} + Bu + L \ast (y - C\hat{x})
\]

(5)

\[
\dot{\hat{x}} = (A - L \ast C)\hat{x} + Bu + L \ast y
\]

(6)

\[
\dot{\hat{x}} = \hat{A}\hat{x} + Bu + L \ast y
\]

(7)
Where, $\tilde{A} = A - L \cdot C$, and the Eigen values of $\tilde{A}$ control the error dynamics of the observer.

$L$ is the Luenberger gain and $\hat{x}$ is the estimate of the state $x$ at time $t$.

The poles for the observer for both pitch and yaw are chosen to be at -1, -2, and -3.

These are the Eigen values of the matrix $\tilde{A} = A - L \cdot C$.

By using Ackermann’s Formula

$$|sI - \tilde{A}| = (s + 1) \cdot (s + 2) \cdot (s + 3)$$

$$|sI - (A - L \cdot C)| = (s + 1) \cdot (s + 2) \cdot (s + 3) \quad (8)$$

Where $I$ is an Identity matrix.

Thus by equating LHS to RHS in equation (8), the Luenberger gain $L$ is calculated for both the pitch and the yaw and is given below.

The Luenberger gain $L$ for Pitch is:

$$L = \begin{pmatrix} -2.9012 \\ 11.8917 \\ 2.2713 \end{pmatrix}$$

The Luenberger gain $L$ for Yaw is:

$$L = \begin{pmatrix} 35.3716 \\ 76.5373 \\ 19.7974 \end{pmatrix} \quad (9)$$

A. Neural Network Estimator

To design the estimator for finding the yaw and pitch neural network algorithms are made use. Neural network algorithm is process of finding the unknown yaw and pitch by using a predetermined output. The set these predetermined data is called training data and the method is called training. Training data consist of input data and target data, in the proposed work signal to the main rotor and tail rotor is called the input data and the yaw and pitch corresponding to the signal is called target data. For training 150 x 2 samples were used, these were further divided into training data, validation and testing data with the ratio of 70%, 15% and 15% corresponding.

Estimation based on ANN is based on a time series correlation between the input and the output, also called as the targets. This assumes a black body model, where the dynamics of the system are not known and the forecasting is done only from the input output relationship of the system. In the proposed work back propagation based neural network algorithm consisting of two hidden layers with 6x2 and 4x2 neurons respectively as shown in Figure 4 [27], [28]. Network parameter of the proposed neural network is given in Table 1.

---

**Fig. 4 Structure of neural network model**

**Fig. 5 Plot of fit graph for pitch**

**Fig. 6 Regression graph for pitch training**
Once the estimators are designed using Luenberger and ANN, it is subjected to test individually to analyze the performance. For analyzing the performance it is subjected to test with unit input condition and then with disturbance. Further the error constant analysis is carried on for evaluation of performance based on standard error constants.

### IV. RESULTS AND ANALYSIS

Here the neurons are trained to replicate the behavior of the system by using the given set of data. The back propagation model with a size of 20 neurons are used to predict the output. The plot fit graph and regression graph obtained after training for pitch and yaw is shown in Figure 5, Figure 6, Figure 7 and Figure 8 respectively.

### TABLE I. Neural network parameters

<table>
<thead>
<tr>
<th>OPTIMIZED PARAMETERS OF THE NEURAL NETWORKS MODEL</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Database</td>
<td>--</td>
</tr>
<tr>
<td>Training base</td>
<td>105x2</td>
</tr>
<tr>
<td>Validation base</td>
<td>30</td>
</tr>
<tr>
<td>Test base</td>
<td>30</td>
</tr>
<tr>
<td>No of neurons in</td>
<td></td>
</tr>
<tr>
<td>1st layer</td>
<td>6x2</td>
</tr>
<tr>
<td>2nd layer</td>
<td>4x2</td>
</tr>
<tr>
<td>Activation function</td>
<td></td>
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<tr>
<td>1st layer</td>
<td>tansig</td>
</tr>
<tr>
<td>2nd layer</td>
<td>tansig</td>
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<tr>
<td>Output layer</td>
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<td>Learning rate</td>
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<tr>
<td>MSE</td>
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</tr>
<tr>
<td>epoch</td>
<td>16</td>
</tr>
</tbody>
</table>

Fig. 7 Plot of fit graph for yaw

Fig. 8 Regression graph for pitch training.

Fig. 9 Plot of tracking pitch by designed observer for unit input.

Fig. 10 Plot of tracking pitch by designed observer for disturbance.
Fig. 11 Plot of tracking yaw by designed observer for unit input.

Fig. 12 Plot of tracking yaw by designed observer for unit input.

Fig. 13 Plot of tracking yaw by designed observer for unit input.

Response of designed observer based system is plot in Figure 9, Figure 10, Figure 11, Figure 12, Figure 13 and Figure 14 for step input. Response shows that the system was able to track the actual pitch and yaw accurately. Tracking response with disturbance is also plot. From Figure 9 to and Figure 14 it is clear that the observer based estimator was able to track accurately. Similarly, tracking output for ANN based estimator is shown in Figure 15 and Figure 16, the output shows the ANN based estimator was also able to track the pitch and yaw accurately. To analyze the complete behavior in terms of error the IAE, ISE, and ITAE values are computed.

\[
ISE = \int e^2 dt \tag{10}
\]

\[
IAE = \int |e| dt \tag{11}
\]

\[
ITAE = \int t|e|dt \tag{12}
\]

Where \( e \) - error

\( t \) – Time taken

Fig. 14 Plot of tracking yaw by designed observer for unit input.

Fig. 15 Comparison for ISE, IAE, and ISTE for Pitch estimation
Overall performance can be checked from IAE since this penalizes all kinds of error. ISE penalizes large errors more heavily hence this can be used to check transient errors or errors during oscillatory phase. ITAE penalizes errors that occur after certain time more heavily, hence the errors in steady state are more amplified than the errors in transient phase. The comparative results of all these errors for pitch and yaw are shown in Figure 15 and Figure 16 respectively and Table 2.

V. CONCLUSION

Twin rotor multi input multi output system consists of a coupled system, mimicking the behavior of helicopter. The model helps us to understand the control behavior so as to maintain parameters like pitch yaw and roll. To analyze the behavior it is primarily essential to monitor the system, for monitoring we need to install the sensory system. The paper reported a technique for design and comparison of designed estimator for computation of pitch and yaw in case of TRMS. In the reported work two technique were one with computation of estimator based on observer and other based on ANN. From the graphs shown in Figure 9 to Figure 16 it is seen that both the estimators were able to track pitch and yaw accurately. But it was seen that the observer based technique was giving high error during transients and very low errors when it settled. But in case of ANN though the error during transients was low as compared to that of observer its error during static conditions was high.

The analysis helps to understand the dynamic behavior of the TRMS system for yaw and pitch variation, which can be further extended for roll monitoring as well. The work presented would help to diagnose the fault in monitoring the variables using physical system.

References


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